



# **Trade-Offs and Specialization: An Adaptive Dynamics Approach**

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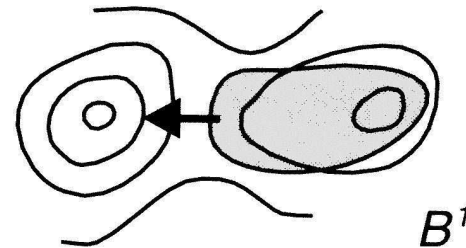
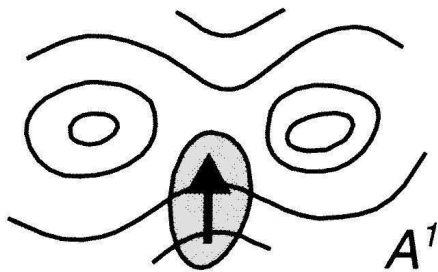
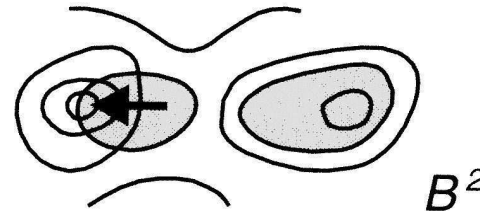
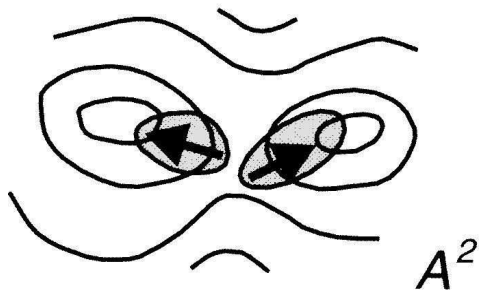
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- ⑥ Some influential older literature treats a two resource situation with fine grained resources.
- ⑥ Many empirical systems might best be approximated by this set up (e.g. Crossbills, Black-bellied Seedcrackers, Purple-throated Caribs, scale eating Cichlids).

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- ⑥ Many empirical systems might best be approximated by this set up (e.g. Crossbills, Black-bellied Seedcrackers, Purple-throated Caribs, scale eating Cichlids).
- ⑥ We re-analyze and extend a model of Wilson & Turelli (1986) using AD approximations.

# Theory So Far

## ⑥ Verbal model by Simpson (1953).

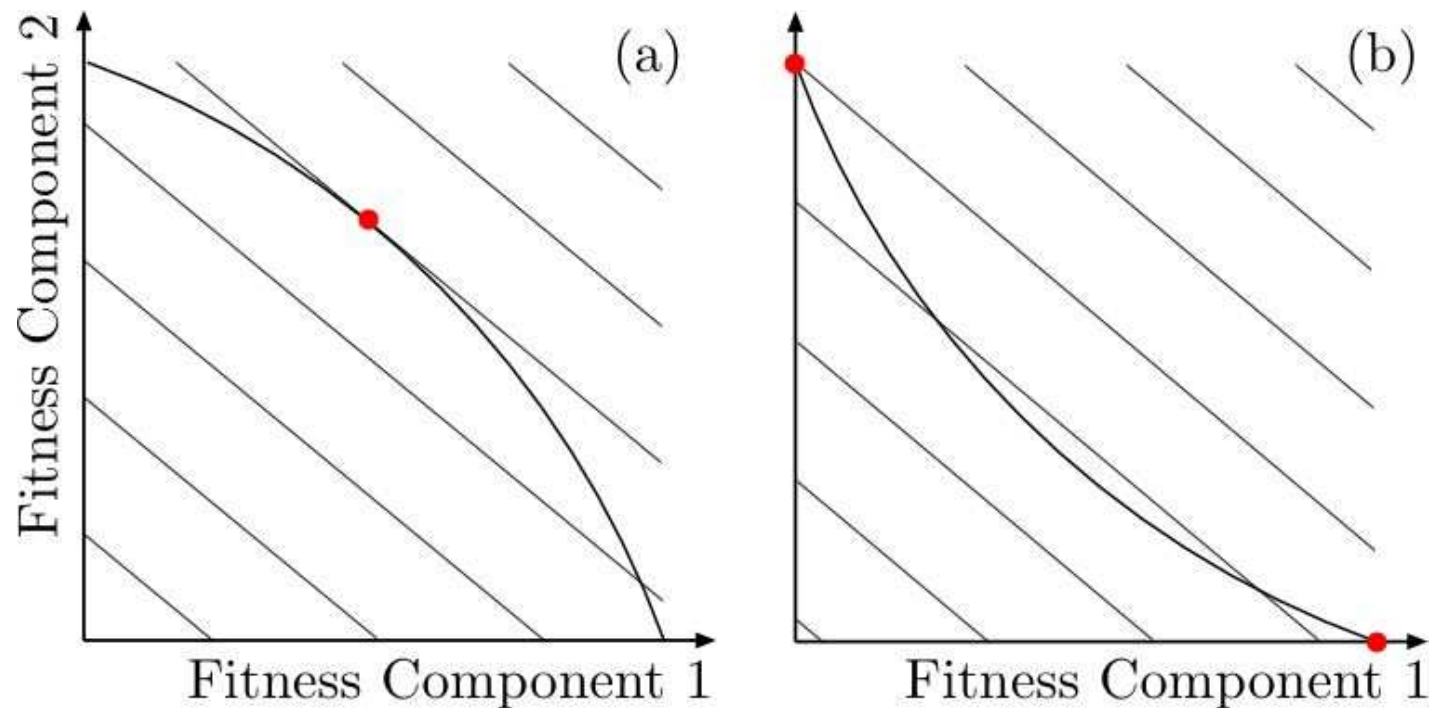


generalist colonizes  
two adaptive peaks

specialist colonizes  
'empty' adaptive peak

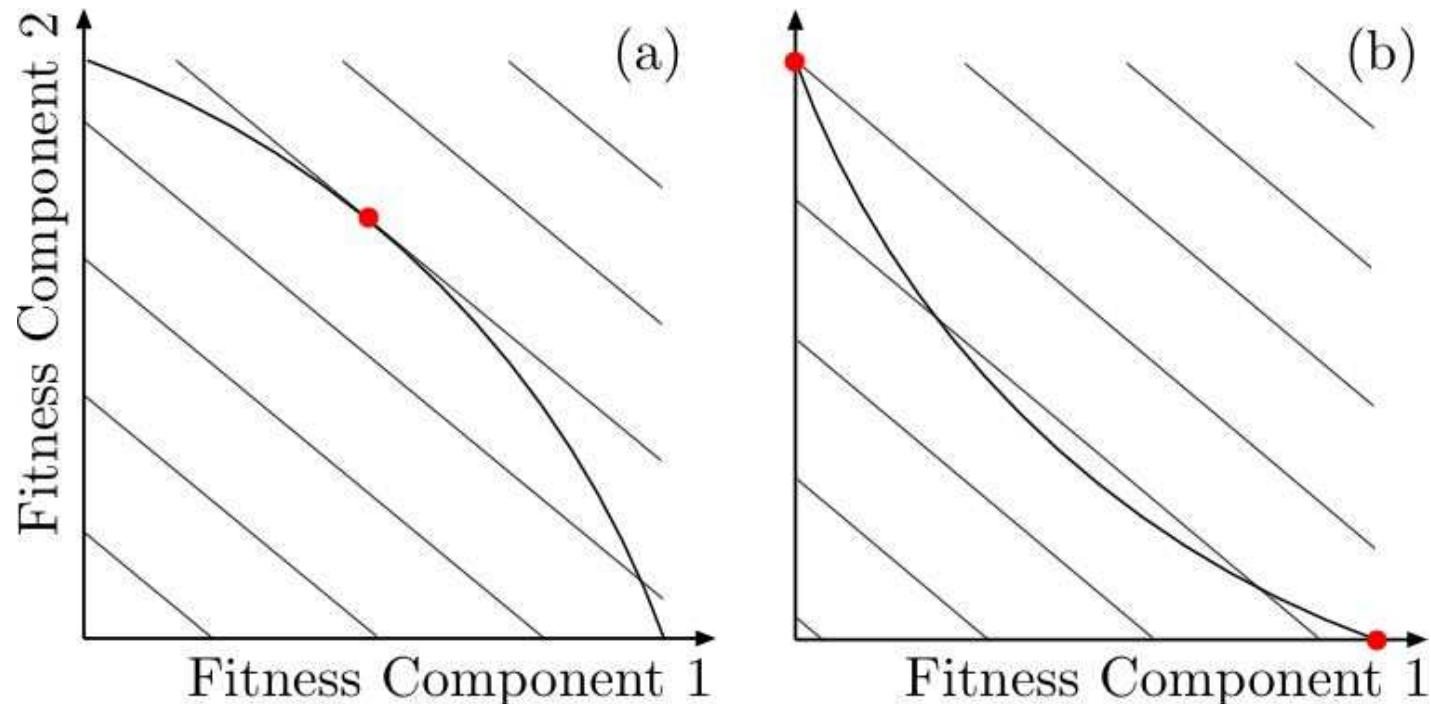
# Levins 1962

- ⑥ Spatially varying environment:  
Convex Phenotype Set  $\implies$  Generalist (a)  
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- ⑥ Spatially varying environment:  
Convex Phenotype Set  $\implies$  Generalist (a)  
Concave Phenotype Set  $\implies$  Specialist (b)
- ⑥ **However:** Levins explicitly excluded density- and frequency dependence  $\implies$  No coexistence possible

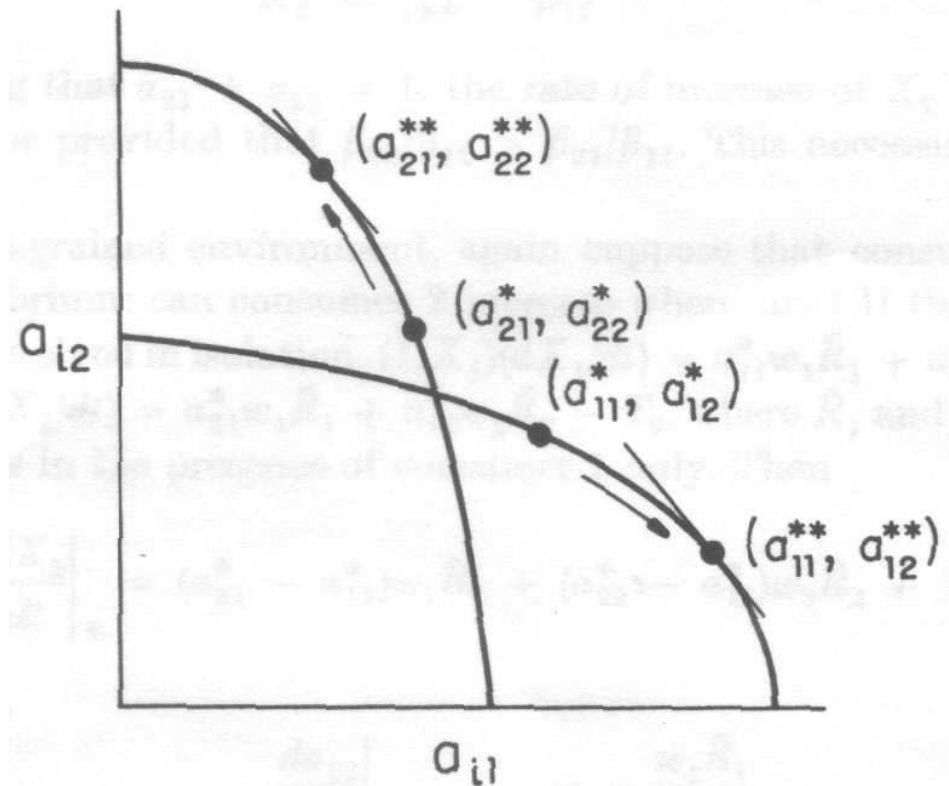




# Lawlor & Maynard Smith 1976,

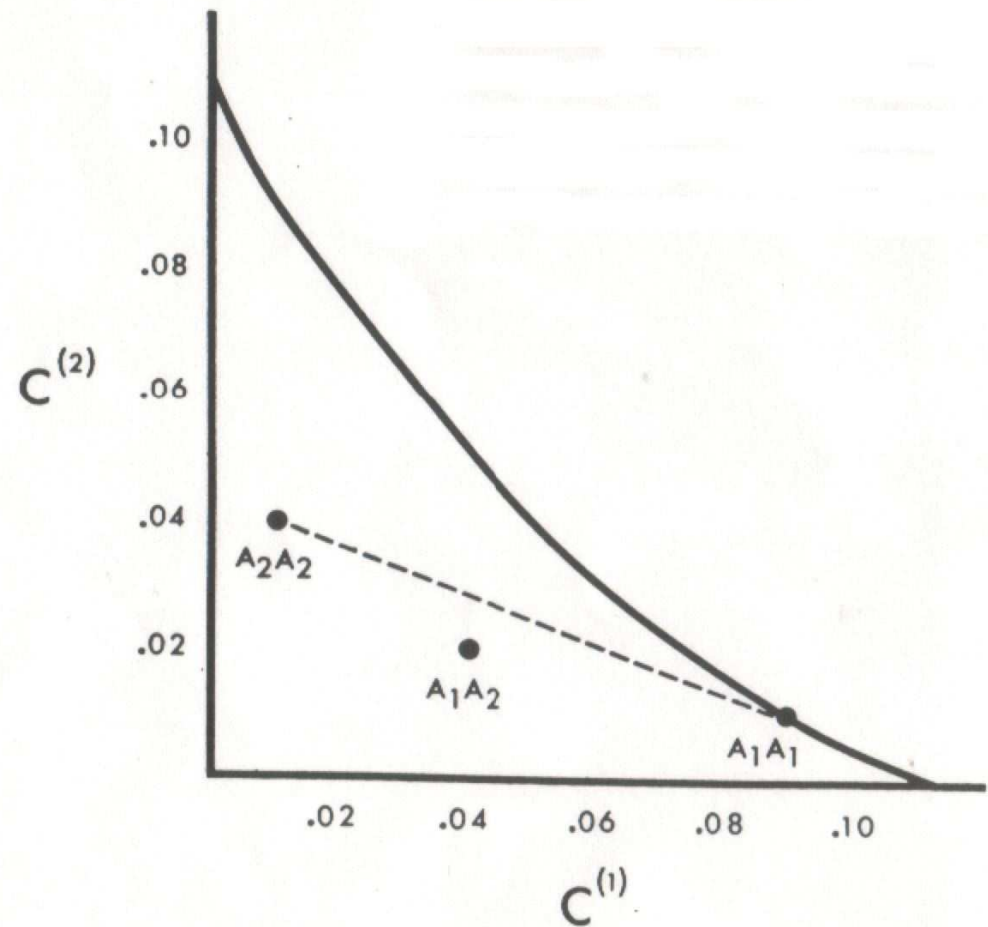
Abrams 1986

- Derived fitness function from explicit resource consumption and renewal.
- Density- and frequency-dependent selection  $\implies$  coexistence.
- Character displacement of ESSs on two convex phenotype sets.



# Wilson & Turelli 1986

- ⑥ Two-alleles on one locus code for two consumption rates.
- ⑥ Homozygote  $A_1A_1$  well adapted to resource 1 but poor for resource 2.
- ⑥  $A_1A_2$  and  $A_2A_2$  slightly better for resource 2 but much worse for resource 1.
- ⑥ **Stable polymorphism with underdominance**  
Deviations from population genetical equilibrium shift resource abundances to favor rare allele.



# *Open Questions*

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- ⑥ Do polymorphisms arise in all foraging traits?
- ⑥ How does foraging behavior influence evolution?



# The Foraging Process



$$\alpha \frac{eRpf}{1 + eRp(t_p + ft_m)}$$

population growth rate

- $e$  : search efficiency
- $R$  : resource density
- $p$  : probability of attack
- $f$  : capture success
- $t_p$  : pursuit time
- $t_m$  : manipulation time
- $\alpha$  : conversion factor of prey into offspring

# The Foraging Process II

$$\frac{\alpha_1 e_1 R_1 p_1 f_1 + \alpha_2 e_2 R_2 p_2 f_2}{1 + \underbrace{e_1 R_1 p_1 (t_{p1} + f_1 t_{m1}) + e_2 R_2 p_2 (t_{p2} + f_2 t_{m2})}_{\text{population growth rate on two resources}}}$$

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$p$  : probability of attack

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$t_p$  : pursuit time

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# The Foraging Process III

Without prey choice ( $p_1 = 1 = p_2$ ) and negligible pursuit time  $t_p$ , population growth rate simplifies to:

$$\frac{\alpha_1 e_1 R_1 + \alpha_2 e_2 R_2}{1 + e_1 R_1 t_{m1} + e_2 R_2 t_{m2}} = t_s (\alpha_1 e_1 R_1 + \alpha_2 e_2 R_2)$$

population growth rate on two resources

$e$  : search efficiency

$R$  : resource density

$t_m$  : manipulation time

$\alpha$  : conversion factor of prey into offspring

$t_s$  : search time

# Resource Dynamics

- ⑥ Resource abundance  $R_i$  derived from chemostat dynamics and in quasi steady state:

$$\hat{R}_i = \frac{b_i}{d_i + e_i p_i f_i t_s N}$$

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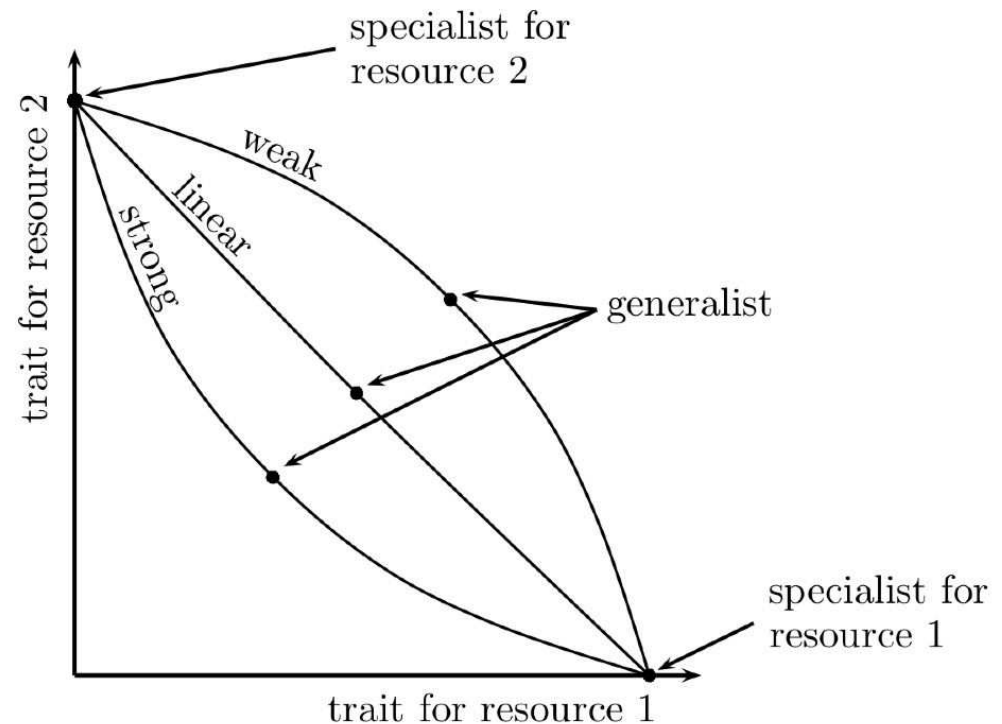
$$\hat{R}_i = \frac{b_i}{d_i + e_i p_i f_i t_s N}$$

- Note:**

- 1)  $e_i, p_i$  and  $f_i$  influence resource abundance  $\hat{R}_i$  explicit
- 2)  $t_{pi}, t_{mi}$  and  $\alpha_i$  influence  $\hat{R}_i$  only implicit via consumer population size  $N$  and search time  $t_s$  and therefore both resources in the same way.

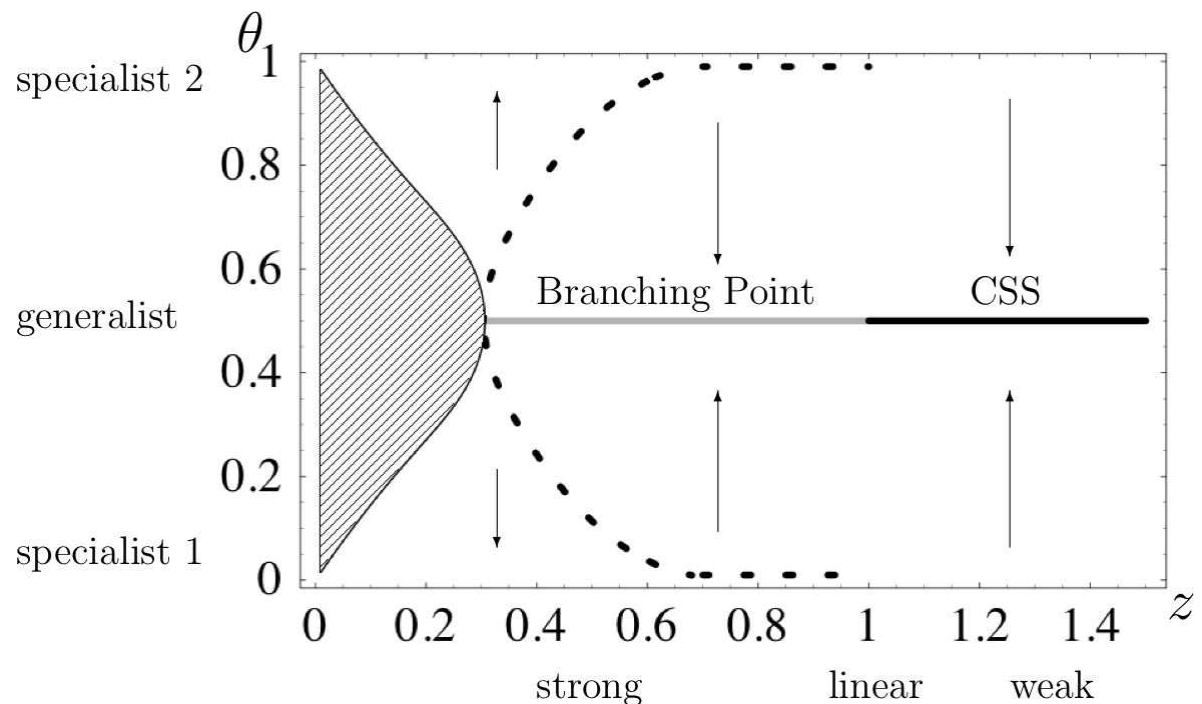
# The Trade-Off

- ⑥ Foraging success is determined by morphological and physiological traits.
- ⑥ Predators face a trade-off  
⇒ they cannot be specialized on two prey-types.
- ⑥ Evolution proceeds along the trade-off curve  
⇒ one-dimensional trait space, parameterized in  $\theta \in [0, 1]$
- ⑥ We concentrate on trade-offs in:
  - in manipulation time  $t_m$
  - in capture success  $f$



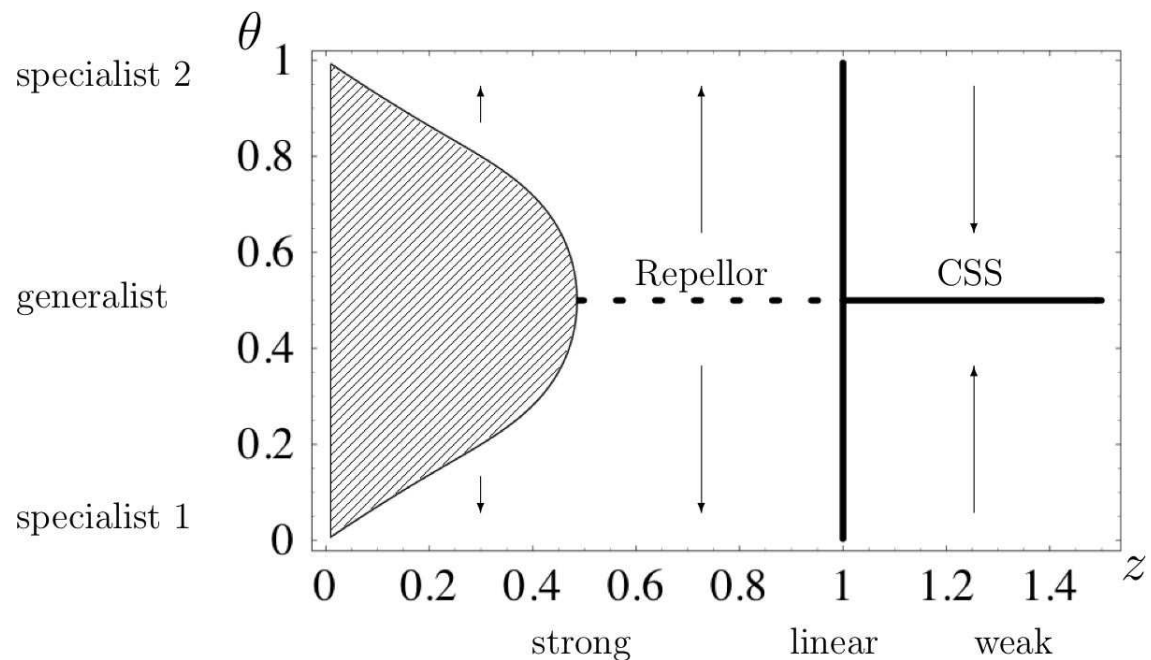
# Trade-Off in Capture Success $f$

- ⑥ Weak trade-off: generalist is CSS.
- ⑥ Strong trade-off: monomorphic population evolves towards generalist. Selection turns disruptive  $\implies$  **branching point**.
- ⑥ Very strong trade-off: only populations close to BP evolve towards it. Otherwise specialization. Coexistence with other specialist still possible.
- Same result for trade-off in search efficiency  $e$ .



# Trade-Off in Manipulation Time $t_m$

- ⑥ No frequency-dependence, no coexistence.
- ⑥ Strong trade-off: both specialists are CSS. Realized CSS depends on initial conditions.
- ⑥ Weak trade-off: generalist is CSS
- Same result for trade-off in pursuit time  $t_p$  and conversion efficiency  $\alpha$ .





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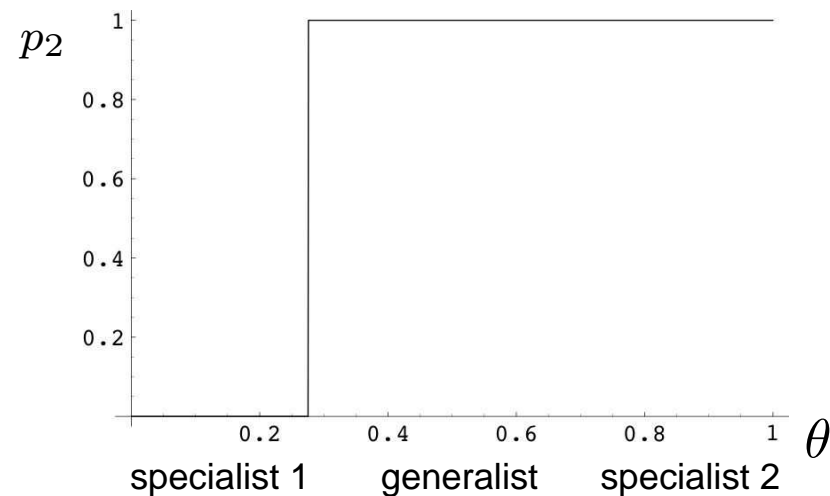
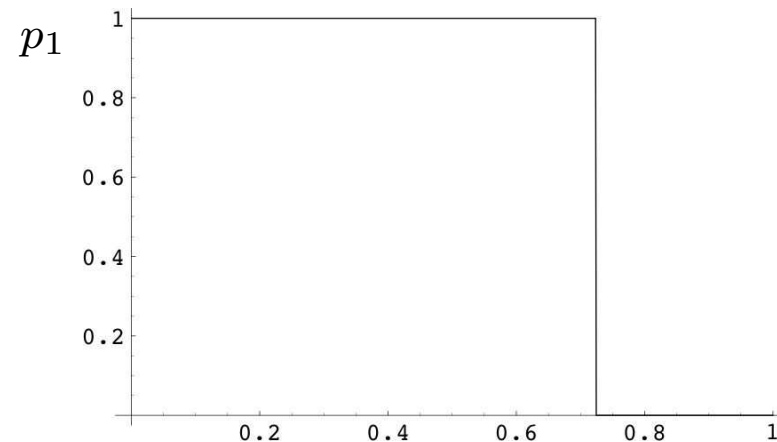
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- ⑥ **Extension:** including diet choice applying optimal foraging theory.

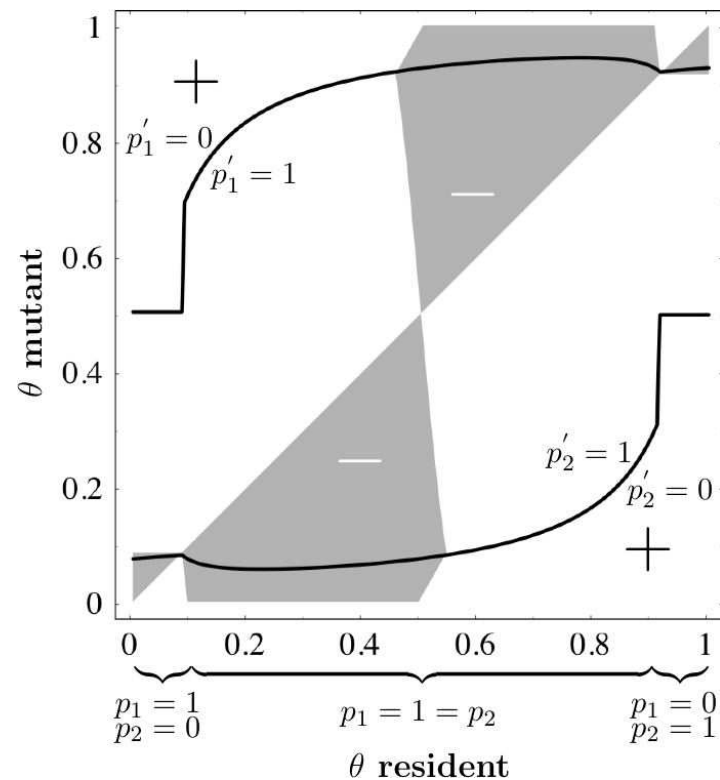
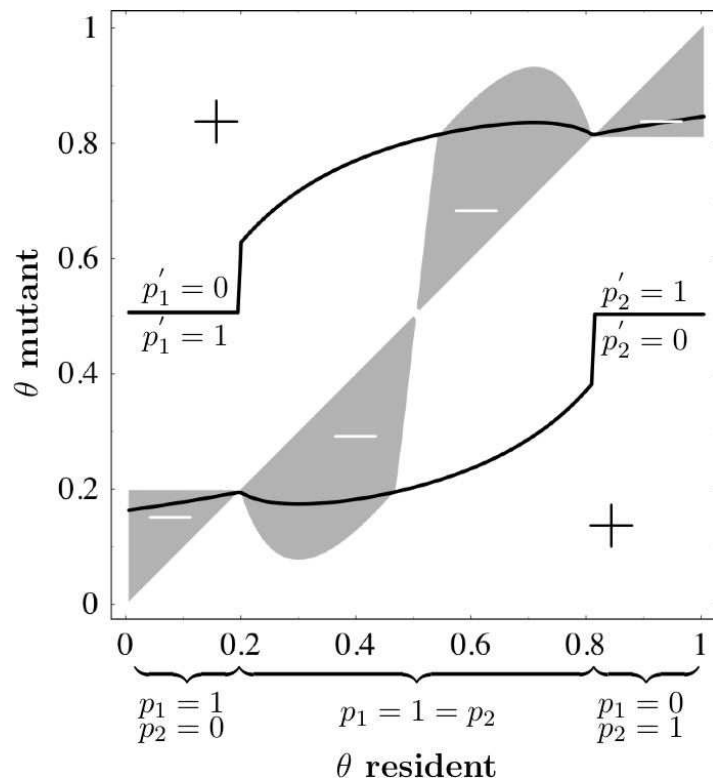
# Optimal Diet Choice

- ⑥ Prey profitability (fitness gain per investment of time) conditional on genetic trait.
- ⑥ **Zero-one rule:**  
A prey type is either always or never taken.



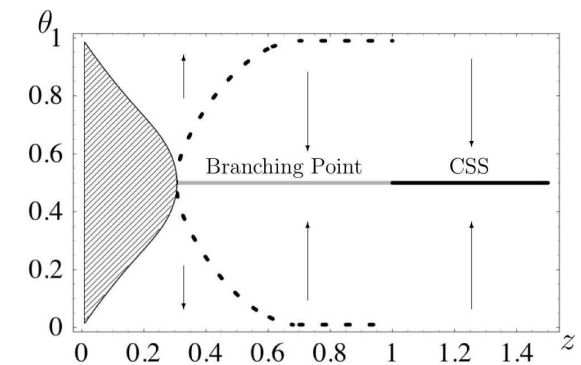
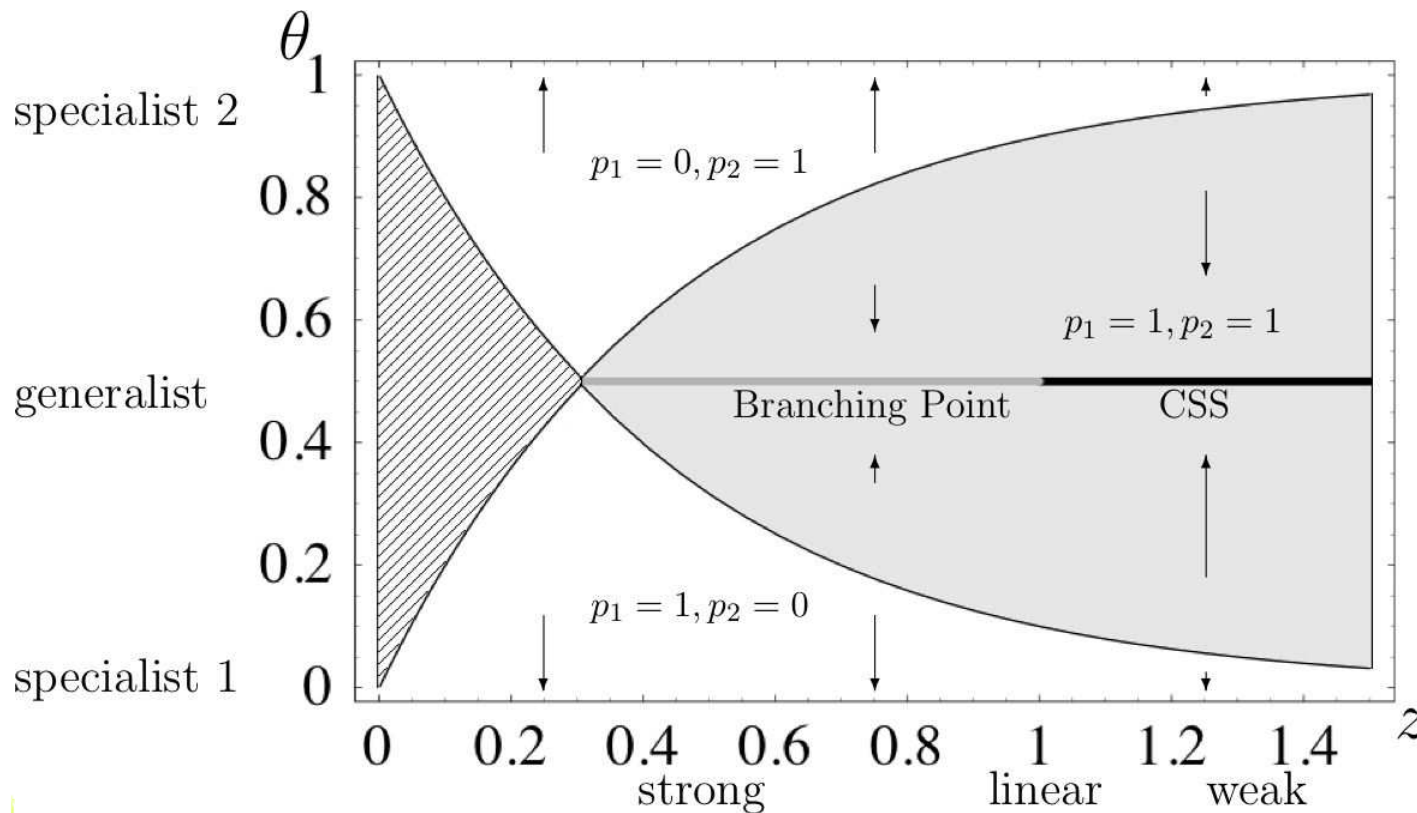
# Extended PIPs: Capture Success

- ⑥ Fitness function is non-differentiable where prey switch takes place.
- ⑥ **Mutant choice boundaries** indicate prey switch of mutant.



# Trade-Off in Capture Success II

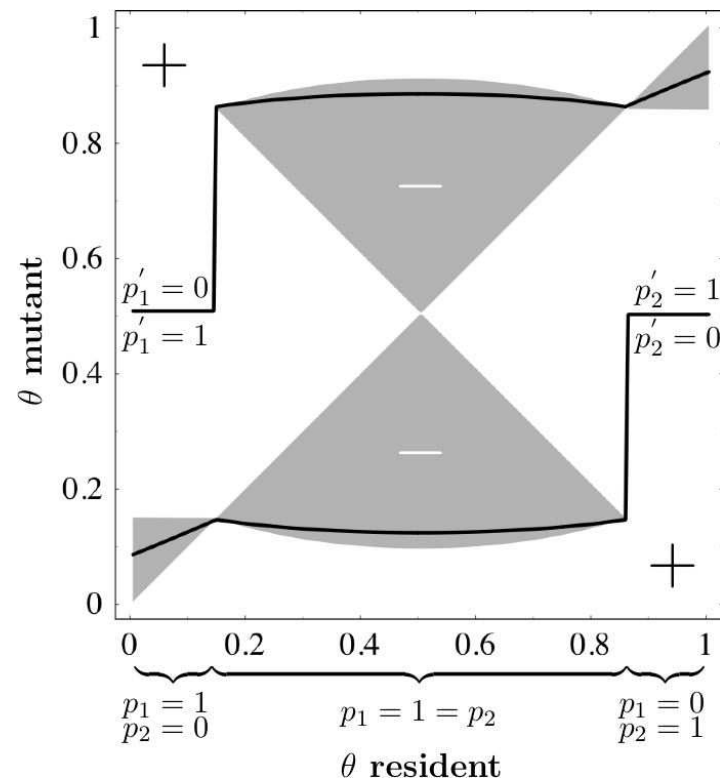
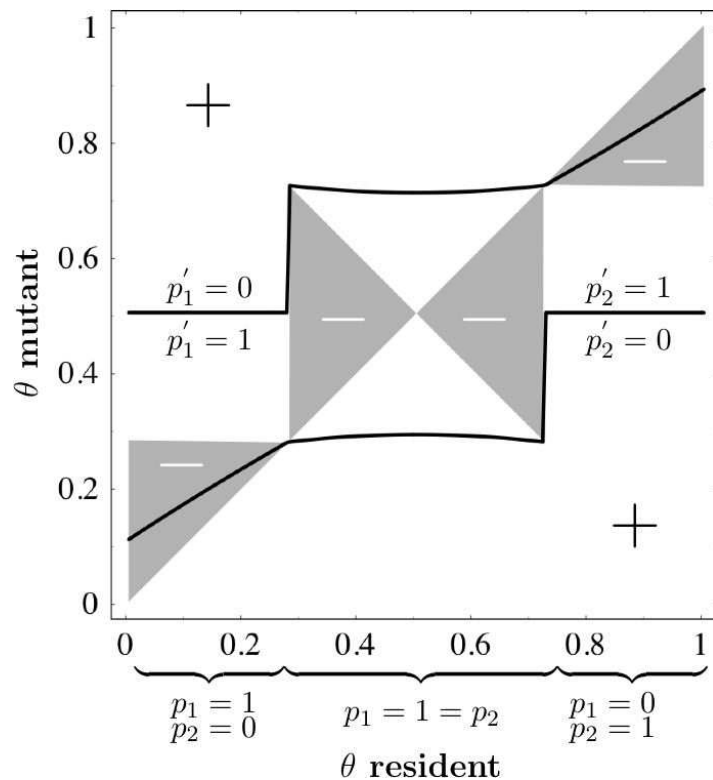
- ⑥ If both resources are chosen  $\implies$  Equals scenario without diet choice
- ⑥ If only one resource is chosen  $\implies$  Specialization





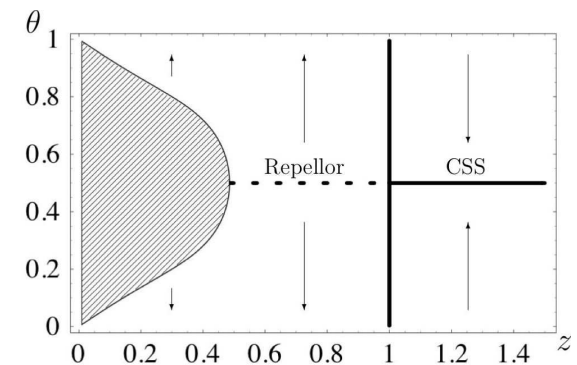
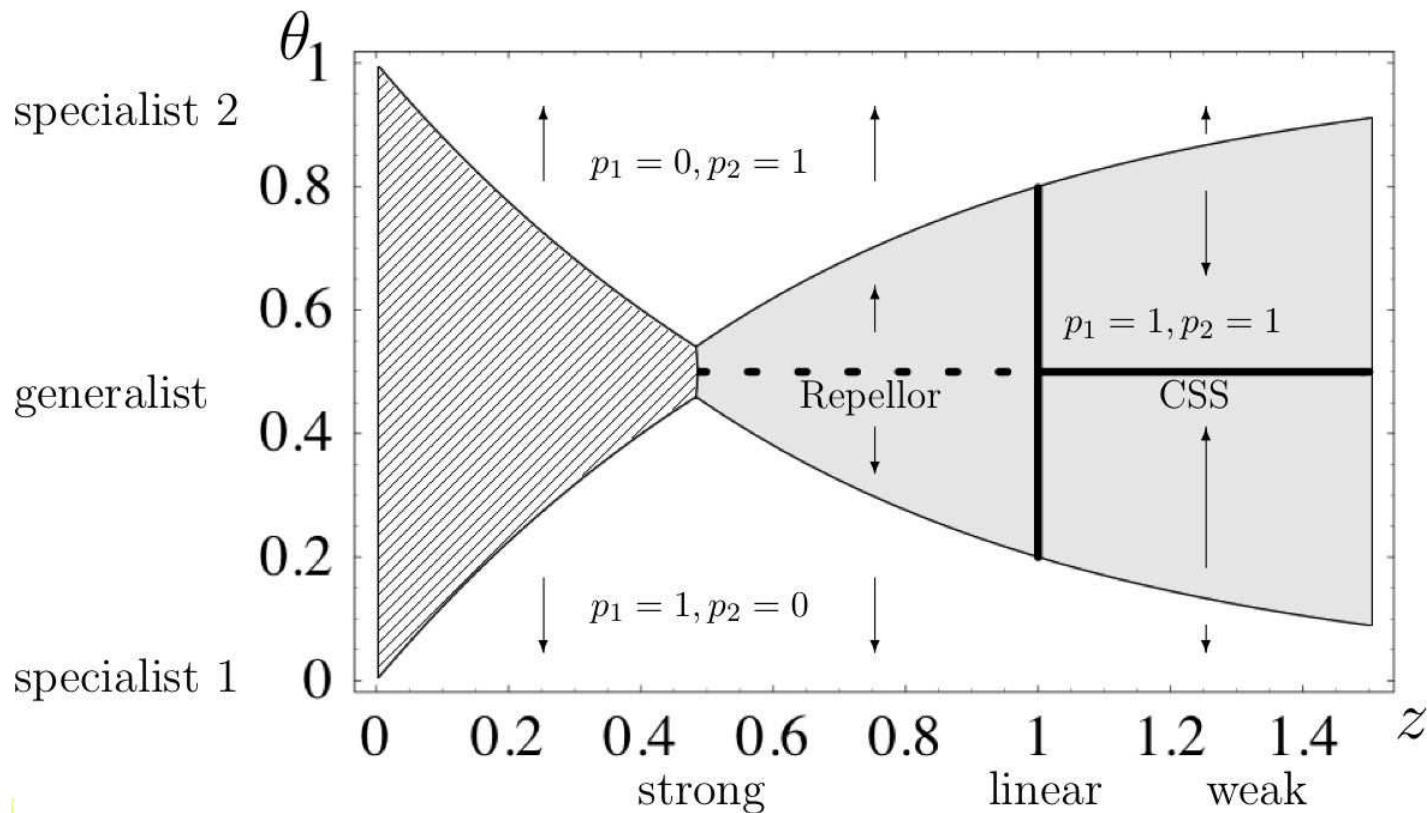
# Extended PIPs: Manipulation Time

- Polymorphisms can emerge through small mutational steps at **non-generic branching points**.



# Trade-Off in Manipulation Time II

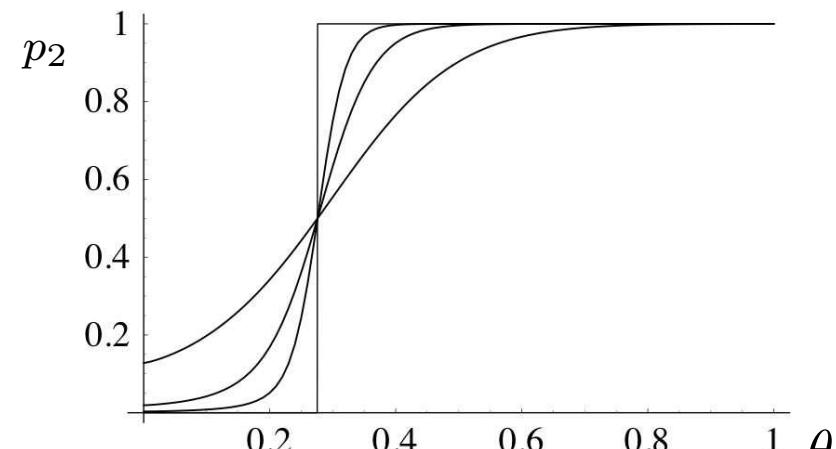
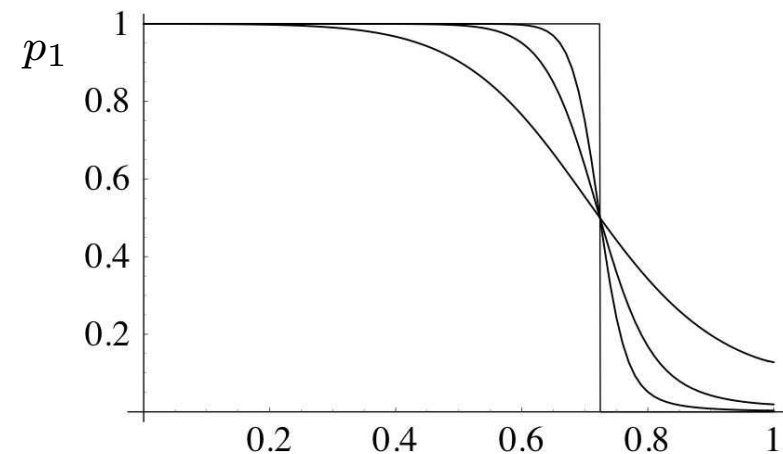
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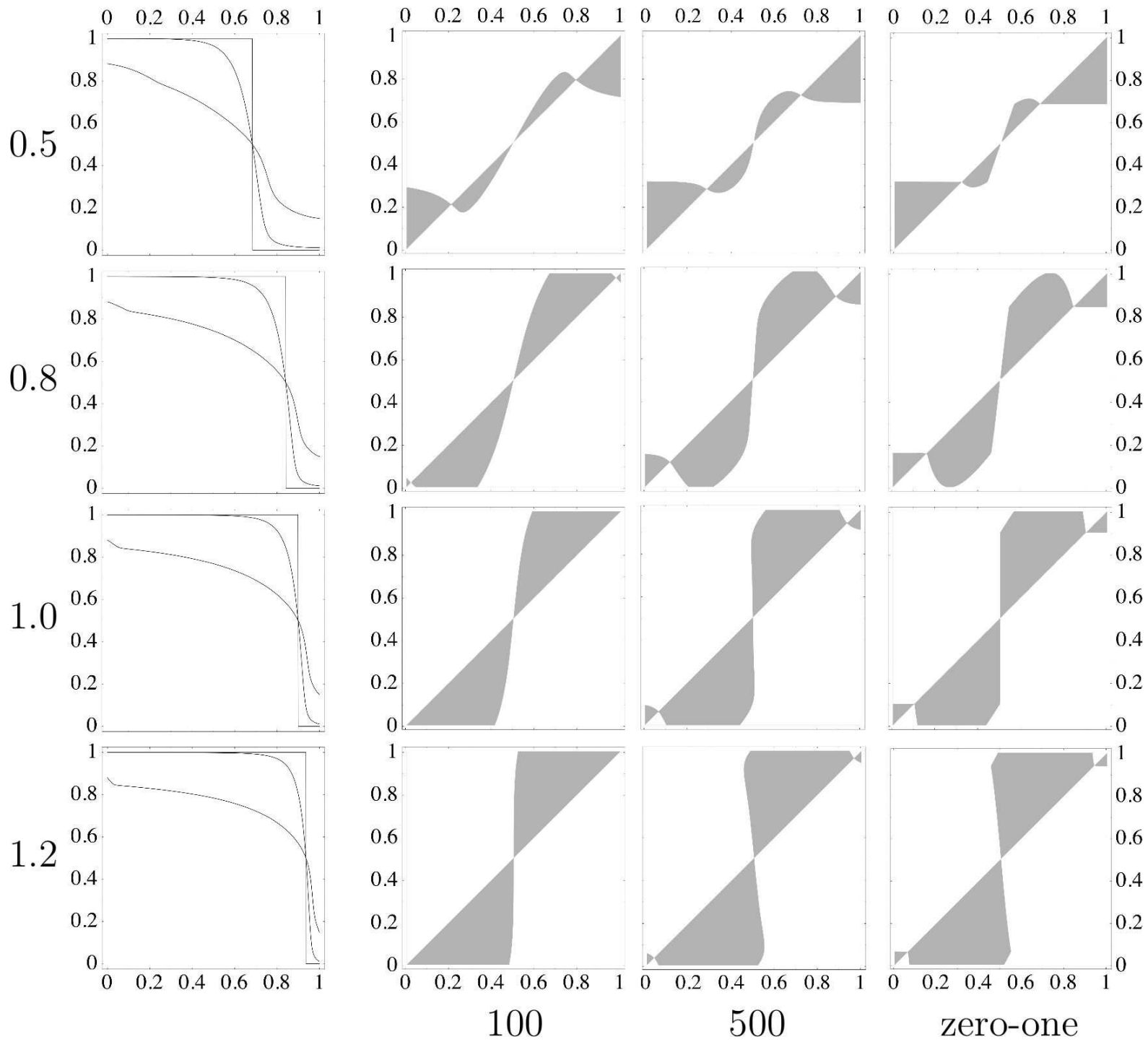


# Foraging Inaccuracy

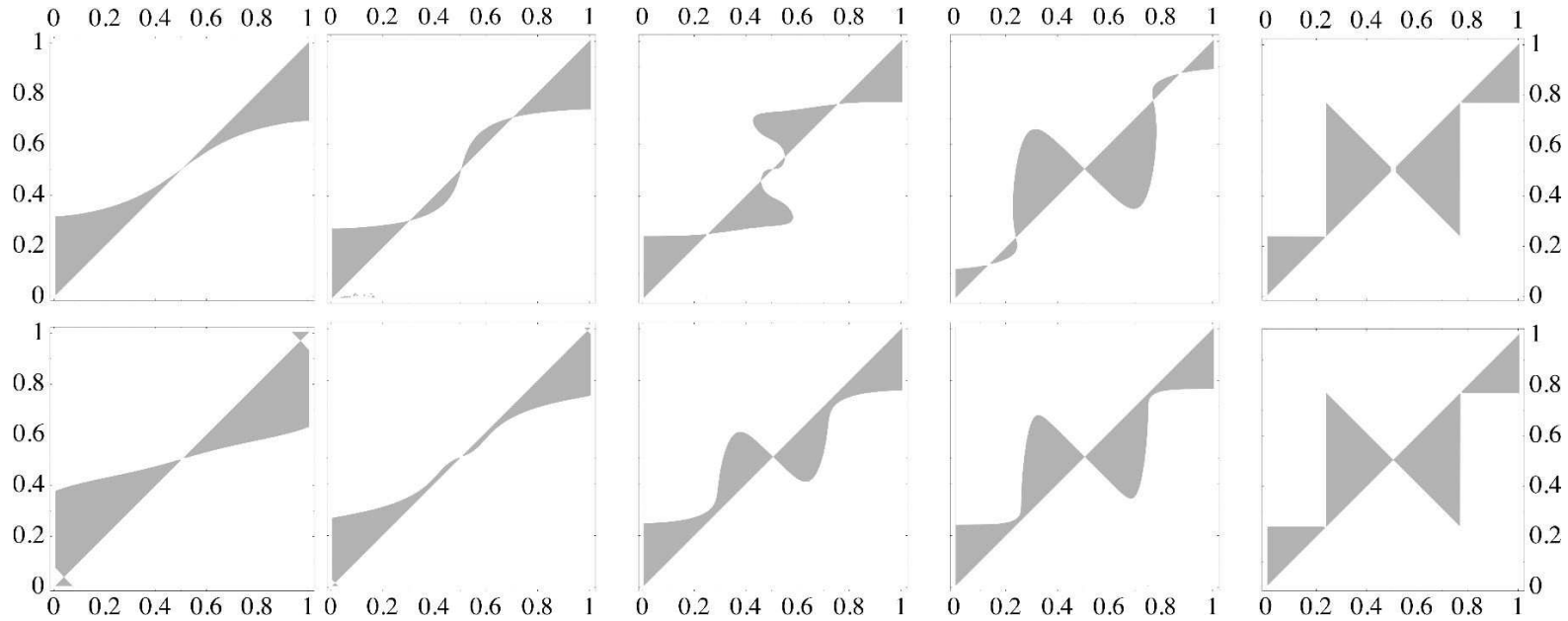


- ⑥ In nature no zero-one rule.
- ⑥ Foraging inaccuracy and incomplete information “smoothens” zero-one rule.
- ⑥ Fitness function becomes differentiable.





# Trade-Off in Manipulation Time

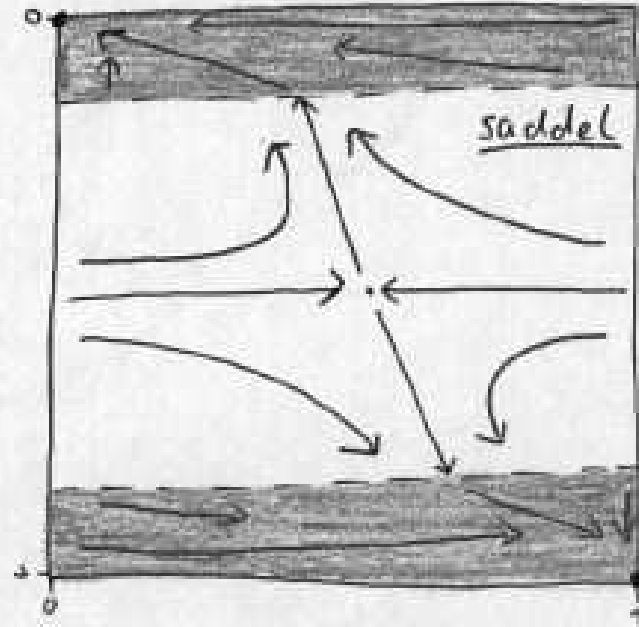
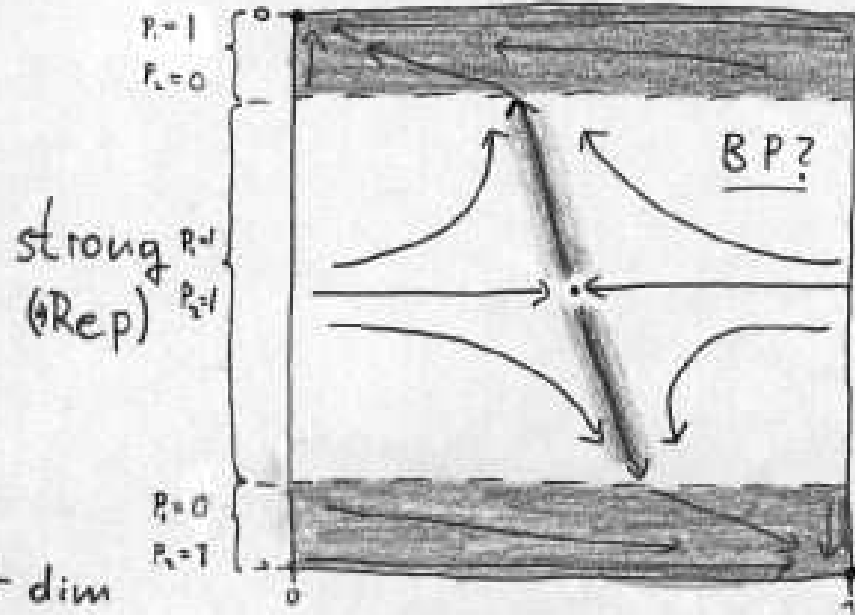


⇒ Increasing Accuracy

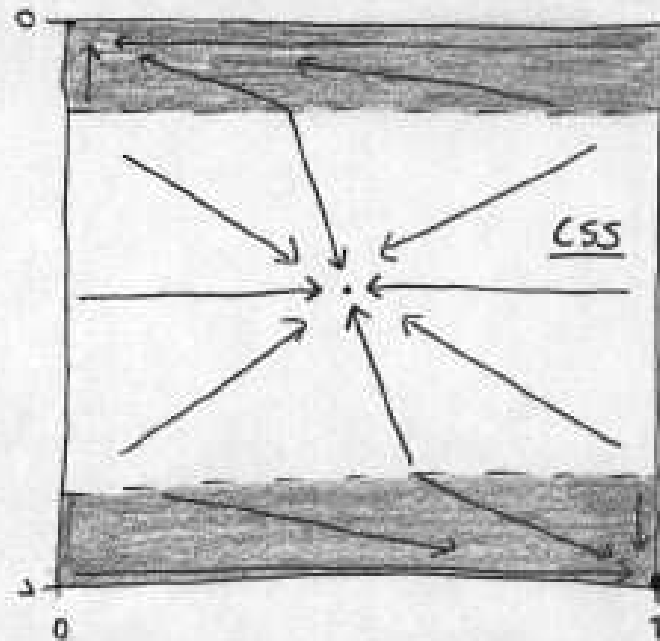
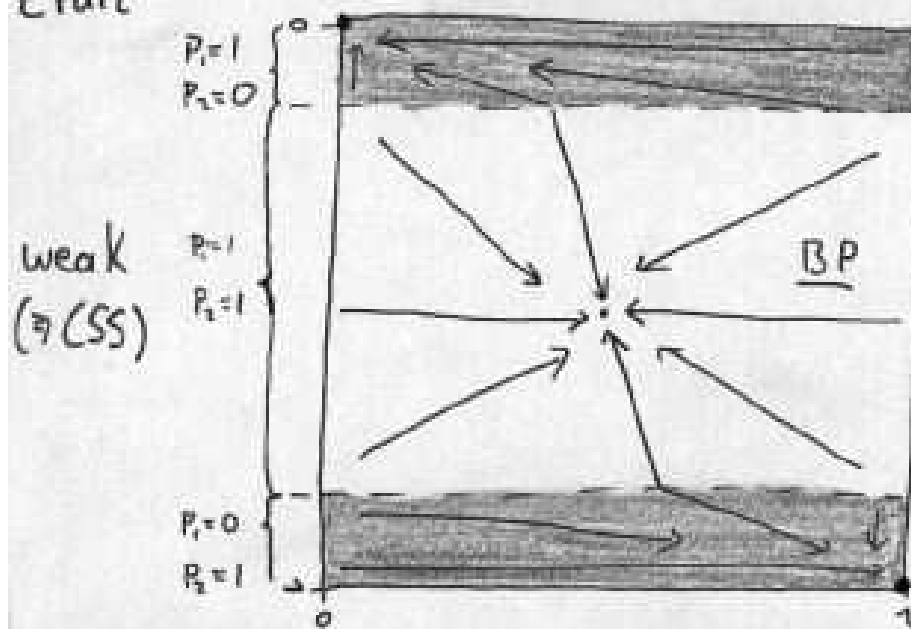
2-dim trait

strong ( $\Rightarrow$  BP)

weak ( $\Rightarrow$  CSS)



1-dim trait



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- ⑥ Prey choice facilitates coexistence and the evolution of polymorphisms.
- ⑥ Which specific type of polymorphism evolves under disruptive selection depends on genetic architecture.
- ⑥ In higher dimensions prey choice can prevent branching.