

## Kvantumfizika

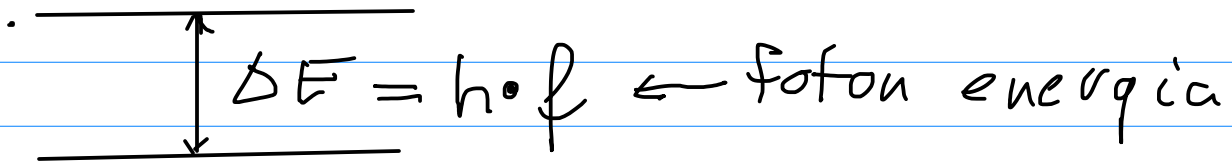
kvantum = energiaadag

Planck állandó:

$$h = 6,63 \cdot 10^{-34} \text{ J}\cdot\text{s}$$

$$\hbar = \frac{h}{2\pi} = 1,05 \cdot 10^{-34} \text{ J}\cdot\text{s}$$

Energiaszintek és elnyelés:



Hullám - részecske

de Broglie összefüggések:

energia:

$$E = h \cdot f = \frac{h}{T} = \hbar \cdot \omega \quad ; \quad \omega = 2\pi \cdot f = \frac{2\pi}{T}$$

impulzus:

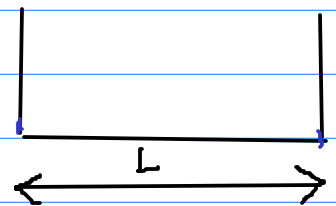
$$p = m \cdot v = \frac{h}{\lambda} = \hbar \cdot k \quad ; \quad k = \frac{2\pi}{\lambda}$$

Dobozba zárt elektron (állóhullám)

$$\lambda = \frac{2L}{n} \quad (n = 1, 2, 3, \dots)$$

$$p = \frac{h}{\lambda} = \frac{h}{2L} \cdot n$$

$$\tilde{E}_n = \frac{1}{2} m v^2 = \frac{p^2}{2m} = \frac{h^2}{8L^2 m} n^2$$



## Harmónikus oszcillátor

### Kvantum harmonikus oszcillátor



$$k = n - 1$$

$$E_k = hf \left( k + \frac{1}{2} \right)$$

---

kvantumszám kétféleképpen:

$n = 1, 2, \dots$  Hány felhullámig osz?

$k = n - 1 = 0, 1, 2, \dots$  Hány csomópont?

(Ez a  $k$  nem ugyanaz, mint a hullámszám  $k$ -ja az előző lapon.)

# Atomi elektronszerkezet

csomófelületek:  $k = l + g$

- csomósík  $l$

- csomógömb  $g$

főkvantumszám  $n = l + 1 = l + g + 1$

melletti kvantumszám:  $l$

$$g = n - 1 - l$$

$$n \geq 1$$

$$0 \leq l \leq n - 1$$

$$0 \leq g$$

|   |     |
|---|-----|
|   | $l$ |
| s | 0   |
| p | 1   |
| d | 2   |
| f | 3   |

Pauli elk: 1 pályán max 2 elektron

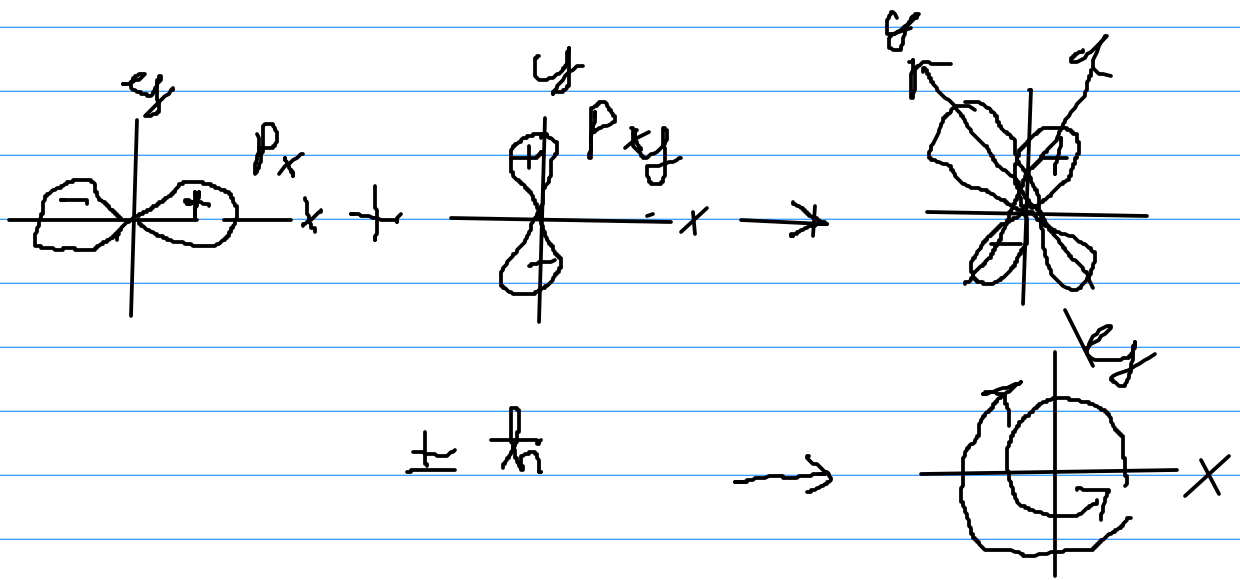
mágneses kvantumszám:  $m$   
pályainkvánság  $-l \leq m \leq l$   $2l + 1$  de  $l \neq 0$ .

Spin kvantumszám:  $s = \pm \frac{1}{2}$

Pauli elk: 1 állapotban max 1 elektron lehet

2 különböző  
Spinnel!

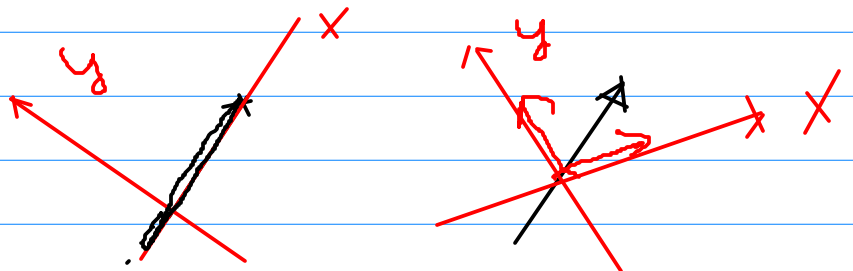
# Superposición de lobe



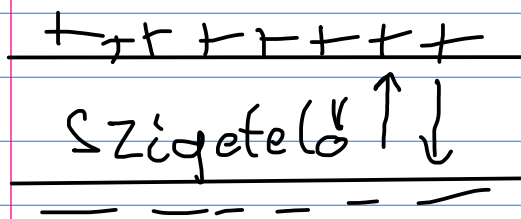
$$m = -1, 0, +1$$

Spin

$$\pm \frac{1}{2} \hbar$$

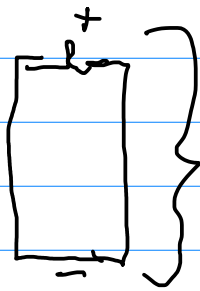


# Elektromosság



kondenzátor

töltés Coulomb C



1,5V

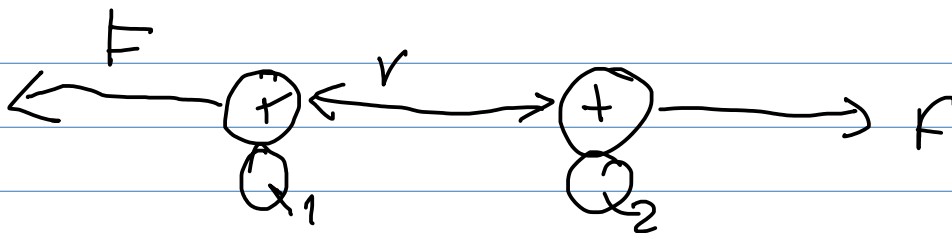
potenciál-  
különbség

~ feszültség

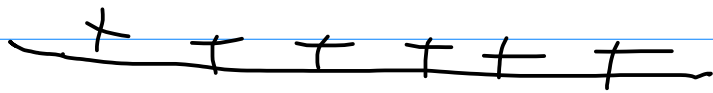
$$C = A \cdot s$$

Amper

$$V = \frac{1}{C} \quad (\text{Volt})$$



$$F = k_e \cdot \frac{Q_1 Q_2}{r^2}$$



$$\oplus Q$$

$$\downarrow F$$



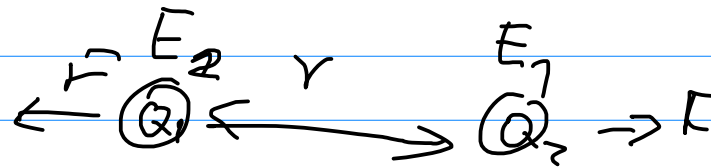
$$F = E \cdot Q$$

$$\uparrow \quad \downarrow C$$

$$E = \frac{N}{C}$$

Coulomb törvénye

$$F = k \frac{Q_1 Q_2}{r^2}$$



gravitációs törvény

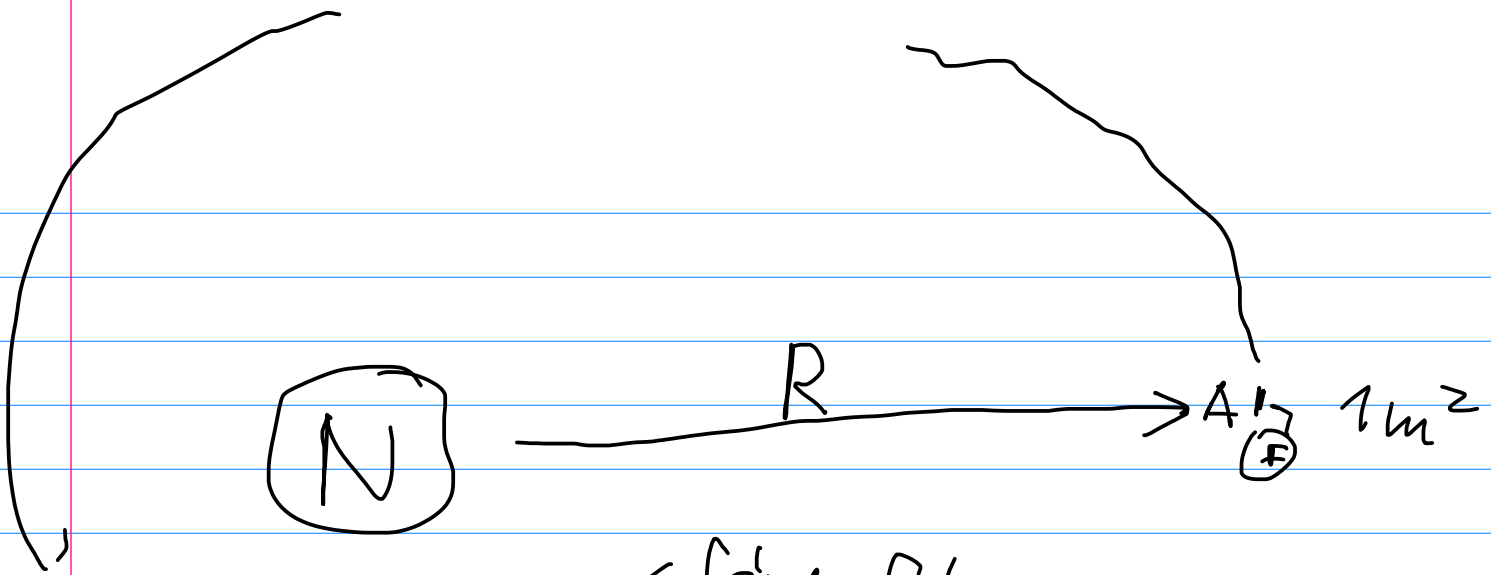
$$F = G \frac{M_1 M_2}{r^2}$$

$$k = 9 \cdot 10^9 \cdot \frac{Nm^2}{C^2}$$

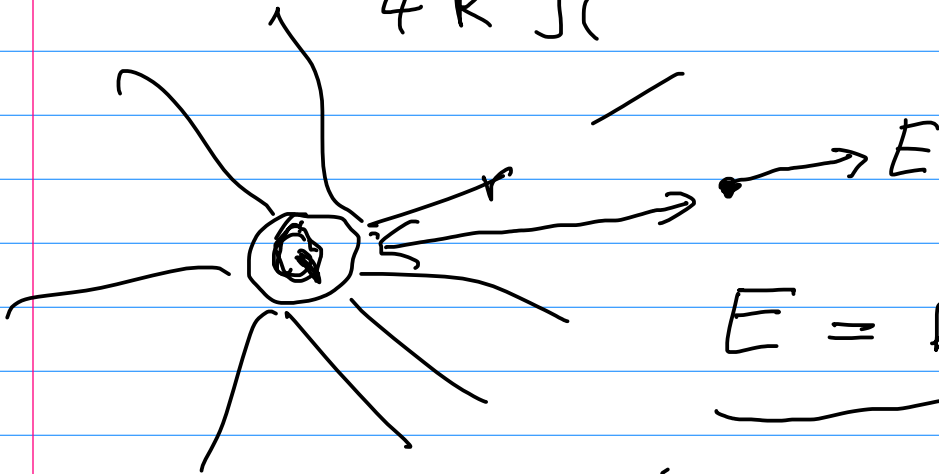
$$\Rightarrow Q_1 \cdot E_2 = Q_2 \cdot E_1$$

$$E_2 = k \cdot \frac{Q_2}{r^2}$$

$$E_1 = k \cdot \frac{Q_1}{r^2}$$



$$P = \frac{\Phi \cdot A}{4R^2 \pi}$$
 ← feny fluxus



$$E = k \frac{Q}{r^2}$$

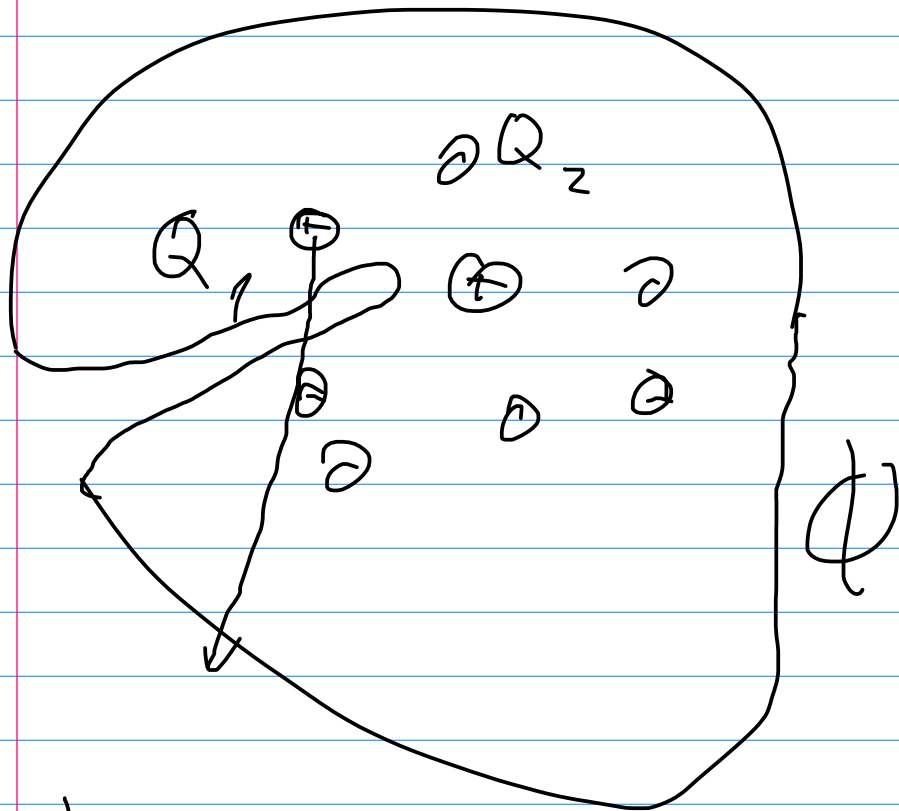
$$E = \frac{\Phi}{4r^2 \pi} = \frac{1}{4\pi \epsilon_0} \cdot \frac{Q}{r^2}$$

elektronos fluxus

$$\Phi = \frac{Q}{\epsilon_0}$$

$$\epsilon_0 = 8,85 \cdot 10^{-12} \frac{C^2}{Nm^2}$$

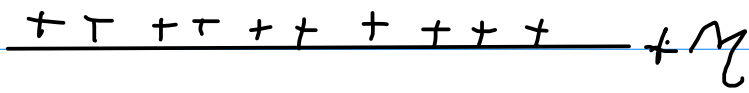
vákuum dielektronos  
állandoja



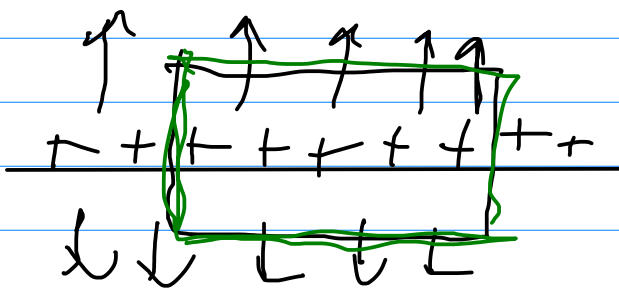
Gauss's law

$$\Phi = \frac{\sum_i Q_i}{\epsilon_0}$$





$$[\sigma] = \frac{C}{m^2}$$



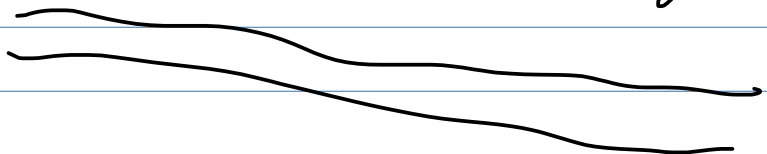
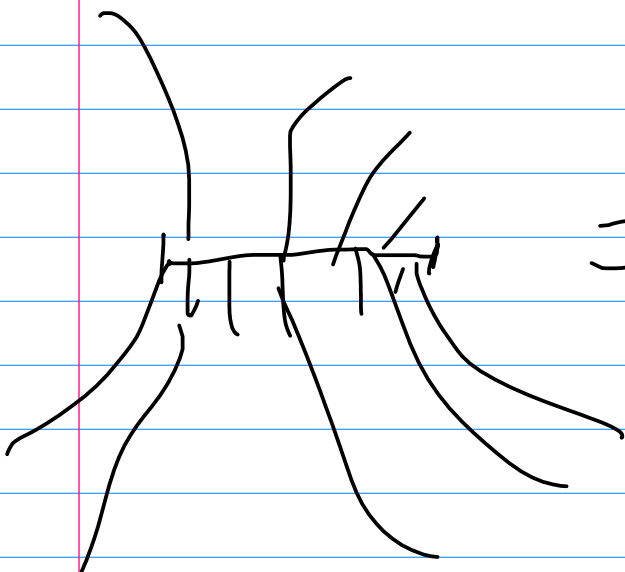
Vegtelesen  
tölftök

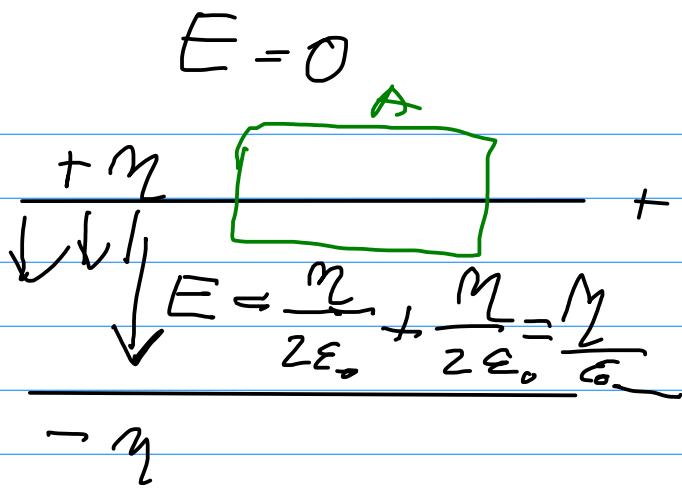
A

$$Q = \sigma \cdot A$$

$$\Phi = \frac{\sigma \cdot A}{\epsilon_0}$$

$$E = \frac{\Phi}{2A} = \frac{\sigma}{2\epsilon_0}$$

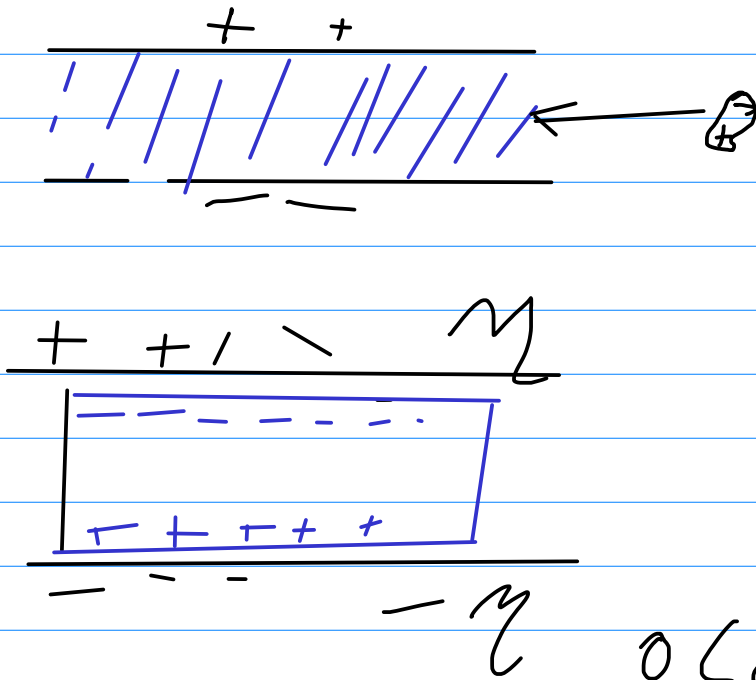




$$\Phi = \frac{QA}{\epsilon_0}$$

$$E = \frac{Q}{\epsilon_0} = \frac{\Phi}{A}$$

$E=0$



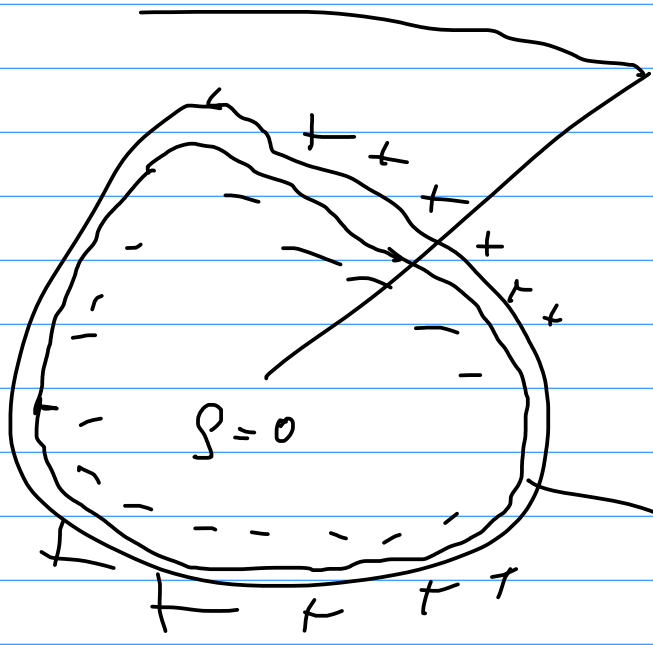
Vakuum dielektrikum

rel. dielektrikum

$$E = \frac{Q}{\epsilon_0 \cdot \epsilon_r}$$

$0 < \epsilon_r < 1$

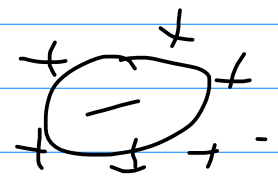
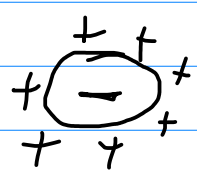
dielektronos all  $\rightarrow E$

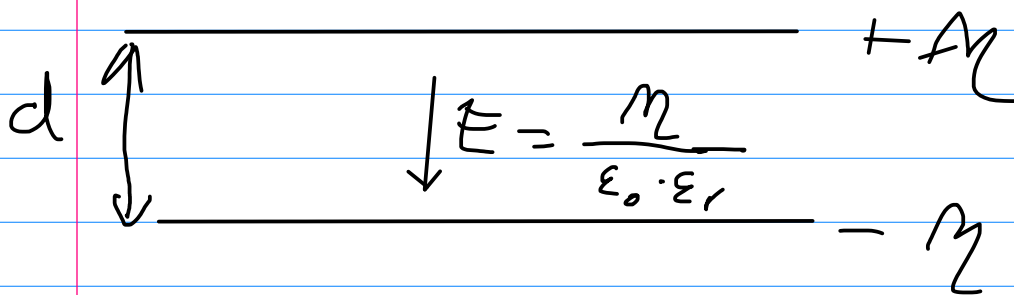


Vizes  
oldat  
"vezező"

szigetelő

$\rho = 0$  ← töltéssűrűség



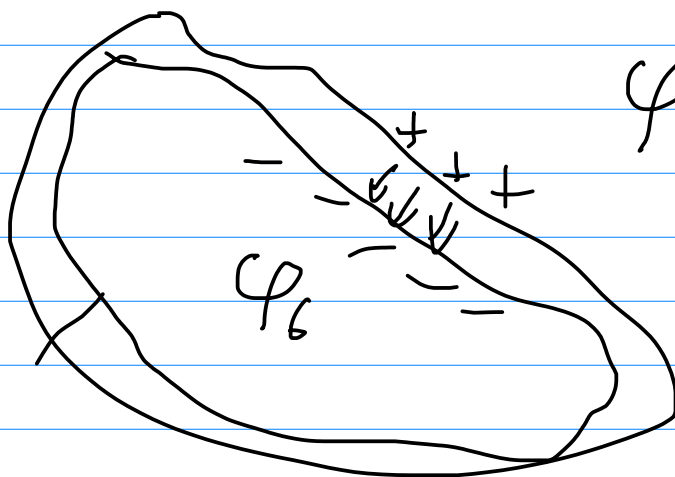


$$\Delta W = F \cdot d = E \cdot Q d = Q \cdot \underbrace{E d}_{\text{feszültségpotenciál-}}$$

különbség  
mértékegysége:

$$[\varphi] = \text{Volt}$$

$$\Delta \varphi = E \cdot d = \frac{M d}{\epsilon_0 \epsilon_r}$$



$$\Delta \varphi = \varphi_0 - \varphi_B = \frac{M d}{\epsilon_0 \epsilon_r}$$